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$v_j = 525 \text{ mph}$
 $\hookrightarrow 235 \text{ m/s}$

$d_y = 30,500 \text{ ft}$
 $\hookrightarrow 9300 \text{ m}$

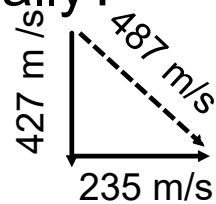
$m = 66.0 \text{ kg}$

$v_y = \sqrt{2g(9300 \text{ m})} = 427 \text{ m/s}$

$p = mv = 66.0 \text{ kg}(487 \text{ m/s})$

$p = 32,200 \text{ kg m/s}$

really?





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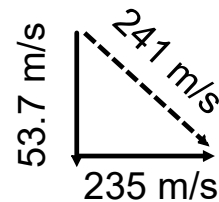
$$m = 66.0 \text{ kg}$$

$$p = mv = 66.0 \text{ kg}(241 \text{ m/s})$$

$$v_y = 120 \text{ mph}$$

$$\quad 53.7 \text{ m/s}$$

$$p = 15,900 \text{ kg m/s}$$



What impulse does an apple give a 45 g bullet traveling at 424 m/s if it slows it to 380 m/s as hits and exits the unfortunate apple? The apple doesn't move upon impact!

$Ft = ?$

$F = ?$

dia. = 11.0 cm



What impulse does an apple give a 45 g bullet traveling at 424 m/s if it slows it to 380 m/s as hits and exits the unfortunate apple? The apple doesn't move upon impact!

- $m_b = 45 \text{ g}$**
- $v_1 = 424 \text{ m/s}$**
- $v_2 = 380 \text{ m/s}$**
- $F_{t_{a-b}} = ?$**



dia. of apple is 11.0 cm (big apple)
 $F = ?$ --- need to find time! d, v, t

$F_{t_{a-b}} = \Delta mv_a$

$Ft = mv_a' - mv_a$

$Ft = m(v_a' - v_a)$

$Ft = .045 \text{ kg}(380 \text{ m/s} - 424 \text{ m/s})$

$Ft = -1.98 \text{ N}\cdot\text{s}$

$F_{t_{a-b}} = \Delta mv_a$

$Ft = -1.98 \text{ N}\cdot\text{s}$

$F = \frac{-1.98 \text{ kg m/s}}{.00027 \text{ s}}$

$F = 7200 \text{ N}$



$d = v_{ave}t$

$t = d/v_{ave}$

$t = .11 \text{ m}/402 \text{ m/s}$

$t = .00027 \text{ s}$

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 $v_1 = 424 \text{ m/s}$
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 dia. of apple is 11.0 cm (big apple)
 $F = ?$

$$Ft = \Delta m v$$

$$Ft = .045 \text{ kg} (380 \text{ m/s} - 424 \text{ m/s})$$

$$Ft = -1.98 \text{ kg} \cdot \text{m/s}$$



$$d = \bar{v} t$$

$$t = \frac{d}{\bar{v}} = \frac{.11 \text{ m}}{\left(\frac{424 \text{ m/s} + 380 \text{ m/s}}{2} \right)}$$

$$t = .000272$$

*$F = ma$
 $a = \frac{v_2 - v_1}{t}$*

$$Ft = m \Delta v$$

$$F = \frac{m \Delta v}{t} = \frac{1.98 \text{ kg} \cdot \text{m/s}}{.000272}$$

$$F = \underline{\underline{7300 \text{ N}}}$$

What impulse is applied to a 325 g ball thrown at 91 mph if it is hit and flies out at 105 mph?
 What average force is applied to the ball as it is thrown if the pitcher's wind-up and pitch is 2.1 m? (2 ways to find force?)

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2.1 m?

$$91 \text{ miles/hr} (1 \text{ hr}/3600 \text{ s})(1610 \text{ m/mile}) = 41 \text{ m/s}$$

$$-105 \text{ miles/hr} (1 \text{ hr}/3600 \text{ s})(1610 \text{ m/mile}) = -47 \text{ m/s}$$

$$Ft = mv = m(v_2 - v_1)$$

$$Ft = .325 \text{ kg}[-47 \text{ m/s} - (41 \text{ m/s})] = -28.6 \text{ kg m/s}$$

$$t = d/\bar{v} = 2.1 \text{ m} / (20.5 \text{ m/s}) = .102 \text{ s}$$

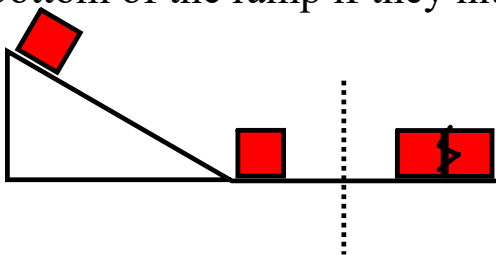
$$Ft = mv \quad F = mv/t = .325 \text{ kg}(41 \text{ m/s})/.102 \text{ s} = 131 \text{ N}$$



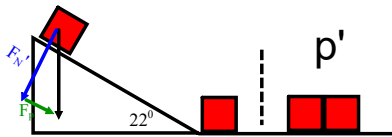
$$a = v^2/2d = (41 \text{ m/s})^2/[2(2.1 \text{ m})] = 400 \text{ m/s}^2$$

$$\text{or, } F = ma = .325 \text{ kg}(400 \text{ m/s}^2) = 130 \text{ N}$$

A 13.5 kg box slides down a 22.0° ramp that is 2.55 m long. What is the speed of the box at the bottom of the ramp if μ is .330? What velocity does it give an identical box at the bottom of the ramp if they hit and stick together?



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$$m = 13.5 \text{ kg}$$

$$F_w = 132 \text{ N}$$

$$d = 2.55 \text{ m}$$

$$\theta = 22.0^\circ$$

$$\mu = .330$$

$$F_{N'} = \cos 22(132 \text{ N}) = 122 \text{ N}$$

$$F_p = \sin 22(132 \text{ N}) = 49 \text{ N}$$

$$\mu = F_f/F_N \quad F_f = \mu F_N = .33(122 \text{ N}) = -40. \text{ N}$$

$$\Sigma F = F_f + F_p = ma$$

$$a = (F_f + F_p)/m$$

$$a = (-40. \text{ N} + 49 \text{ N}) / 13.5 \text{ kg} = .667 \text{ m/s}^2$$

$$v_2 = \sqrt{2(.667 \text{ m/s}^2)2.55 \text{ m}} = 1.84 \text{ m/s}$$

$$\rho = \rho'$$

$$mv_a + mv_b = mv_a' + mv_b'$$

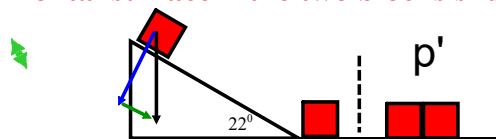
$$mv_a = (m_a + m_b)v'$$

$$mv_a/(m_a + m_b) = v'$$

$$v' = (13.5 \text{ kg} \times 1.84 \text{ m/s}) / (13.5 \text{ kg} + 13.5 \text{ kg})$$

$$v' = .92 \text{ m/s}$$

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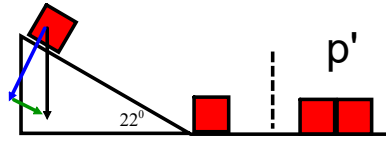
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$$\Sigma F = F_f + F_p = ma$$

$$a = F_f + F_p/m$$

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$$\rho = \rho'$$

$$mv_a + mv_b = mv_a' + mv_b'$$

$$mv_a = (m_a + m_b)v'$$

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$$v' = (13.5 \text{ kg} \times 1.84 \text{ m/s}) / (13.5 \text{ kg} + 13.5 \text{ kg})$$

$$v' = .92 \text{ m/s}$$

$$m = 13.5 \text{ kg}$$

$$F_w = 132 \text{ N}$$

$$d = 2.55 \text{ m}$$

$$\theta = 22.0^\circ$$

$$\mu = .330$$

$$a = v^2/2d$$

$$a = (.92 \text{ m/s})^2 / (2 \times 2.30 \text{ m})$$

$$a = .184 \text{ m/s}^2$$

$$\mu = F_f/F_N = ma/mg = a/g$$

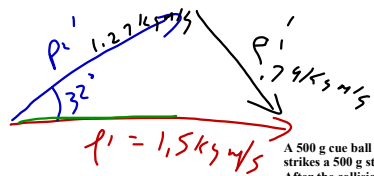
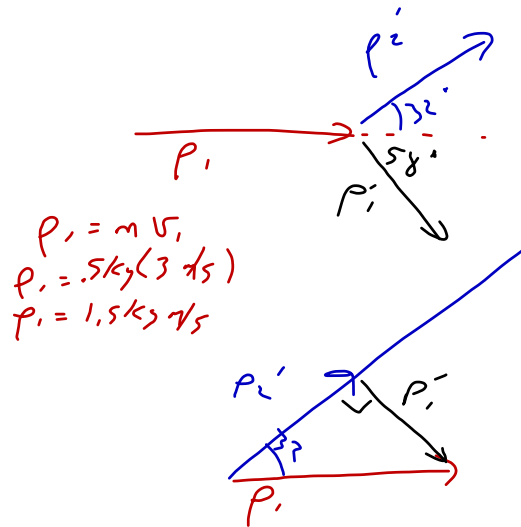
$$\mu = 0.184 \text{ m/s}^2 / 9.81 \text{ m/s}^2$$

$$\mu = .0187$$

A 500 g cue ball traveling at 3.0 m/s strikes a 500 g stationary #2 ball. After the collision the #2 ball takes off at 32 degrees above its original position. What is the momentum and velocity of each ball after the collision?

ex 1

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$$\cos 32 = \frac{p_2'}{1.5 \text{ kg} \cdot \text{m/s}}$$

$$p_2' = \cos 32 (1.5 \text{ kg} \cdot \text{m/s})$$

$$p_2' = 1.27 \text{ kg} \cdot \text{m/s}$$

$$\frac{p_2'}{p_2' = m v_2'}$$

$$v_2' = \frac{p_2'}{m_2} = \frac{1.27 \text{ kg} \cdot \text{m/s}}{.5 \text{ kg}}$$

$$v_2' = 2.54 \text{ m/s}$$

$$\sin 32 = \frac{p_1'}{1.5 \text{ kg} \cdot \text{m/s}}$$

$$p_1' = \sin 32 (1.5 \text{ kg} \cdot \text{m/s})$$

$$p_1' = .79 \text{ kg} \cdot \text{m/s}$$

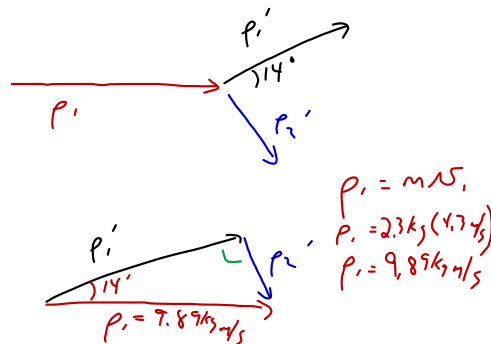
$$p_1' = m v_1'$$

$$v_1' = \frac{p_1'}{m} = \frac{.79 \text{ kg} \cdot \text{m/s}}{.5 \text{ kg}}$$

$$v_1' = 1.58 \text{ m/s}$$

A 2.3 kg ball traveling at 4.3 m/s strikes a stationary ball of 2.9 kg. What are the respective velocities of each ball if the 1st ball takes off at a 14 degree angle after they strike?

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$$p_{1'} = \cos 14 (9.89 \text{ kg} \cdot \text{m/s})$$

$$p_{1'} = 9.60 \text{ kg} \cdot \text{m/s}$$

$$v_{1'} = \frac{p_{1'}}{m} = \frac{9.60 \text{ kg} \cdot \text{m/s}}{2.3 \text{ kg}} = \underline{4.2 \text{ m/s}}$$

$$p_{2'} = \sin 14 (9.89 \text{ kg} \cdot \text{m/s})$$

$$p_{2'} = 2.39 \text{ kg} \cdot \text{m/s}$$

$$v_{2'} = \frac{p_{2'}}{m_2} = \frac{2.39 \text{ kg} \cdot \text{m/s}}{2.9 \text{ kg}}$$

$$\underline{v_{2'} = .83 \text{ m/s}}$$

