

Projectile Motion

Independence of Motion in Two Dimensions

Projectile motion has motion in two dimensions (planes).

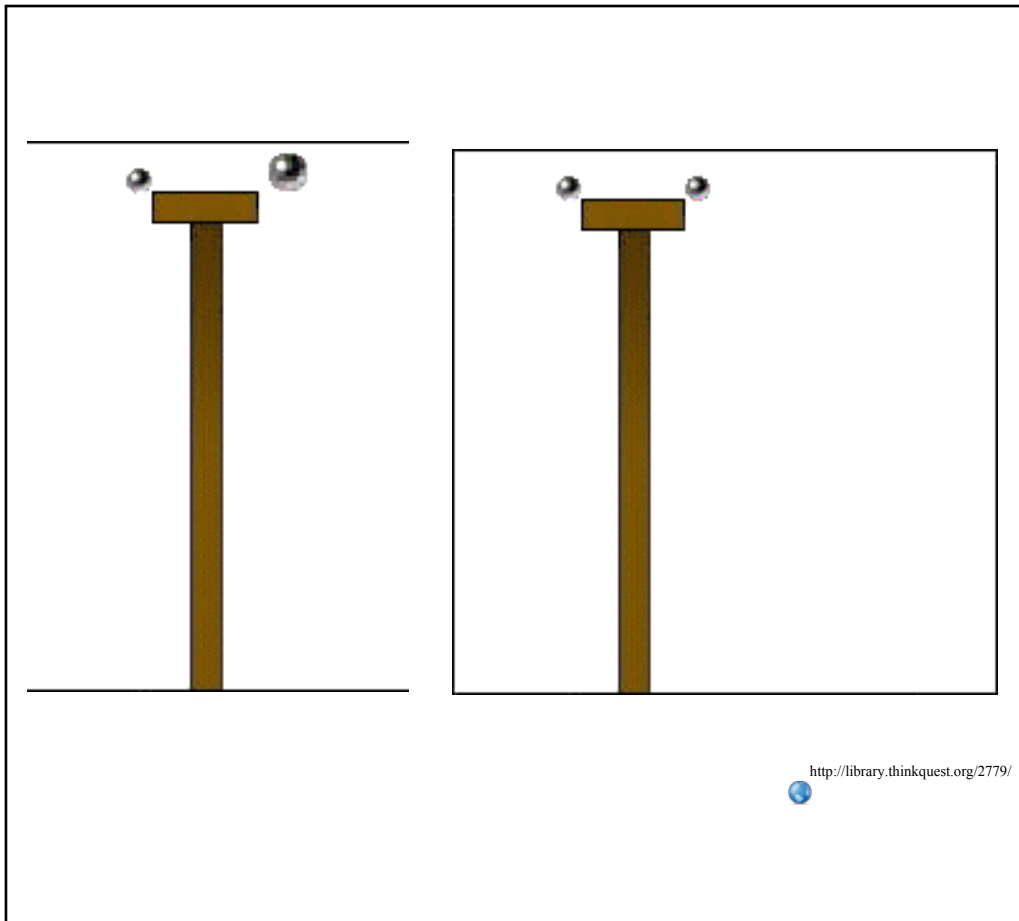
There is motion in the vertical ^y and horizontal ^x at the same time

Because the planes are perpendicular to each other they have no effect of each other.

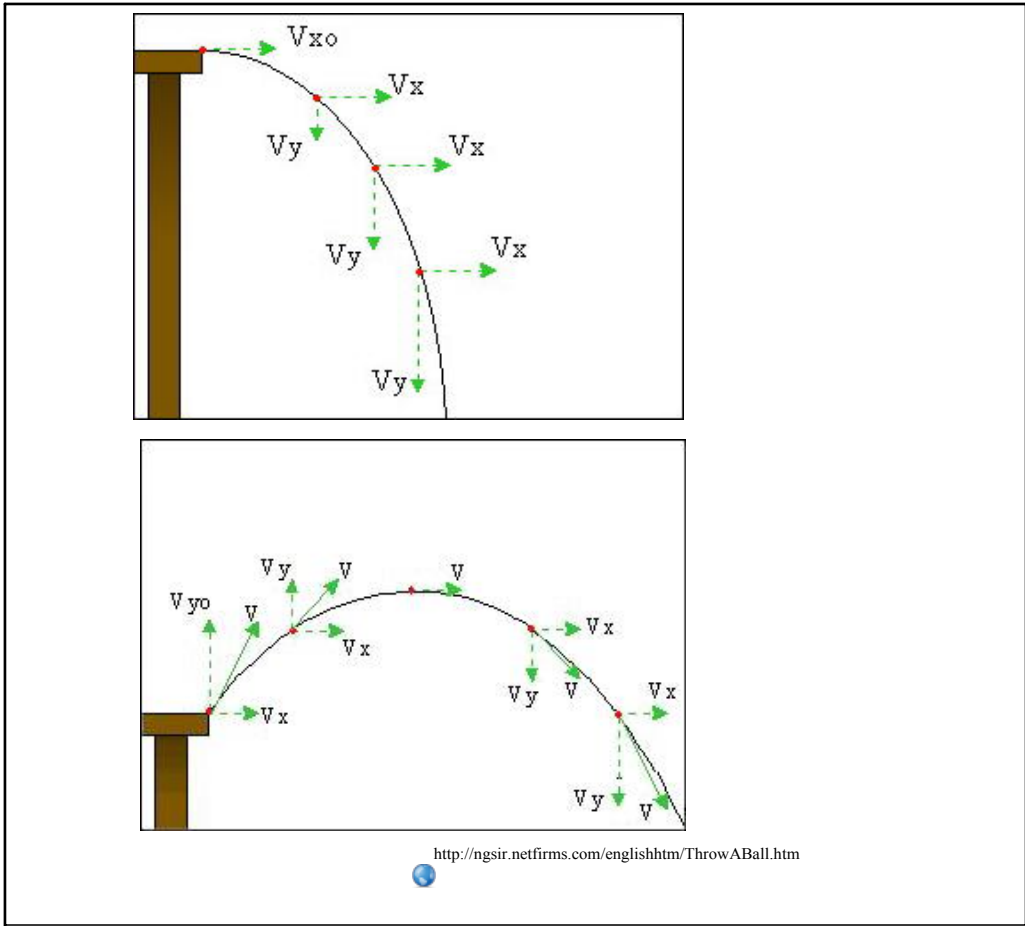
Motion in the "x" does not effect motion in the "y"



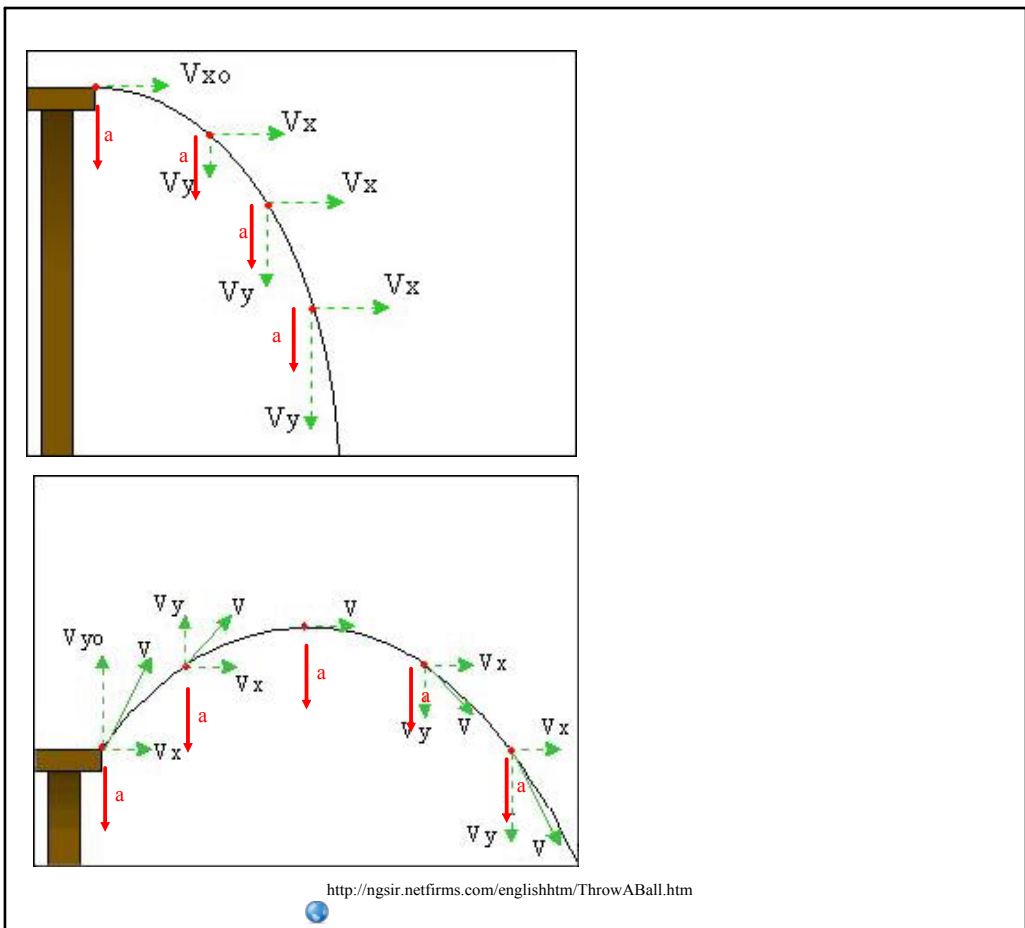
Dec 4-6:28 AM



Nov 14-9:29 AM



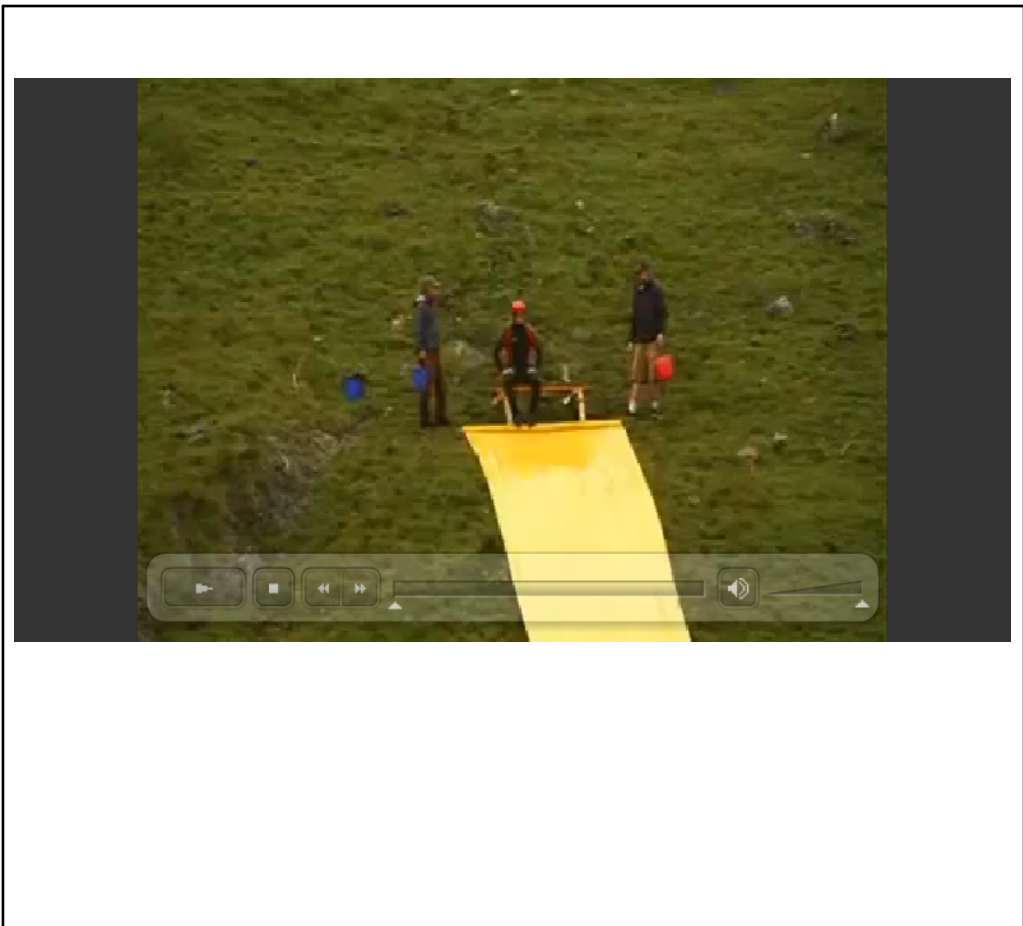
Nov 14-9:30 AM



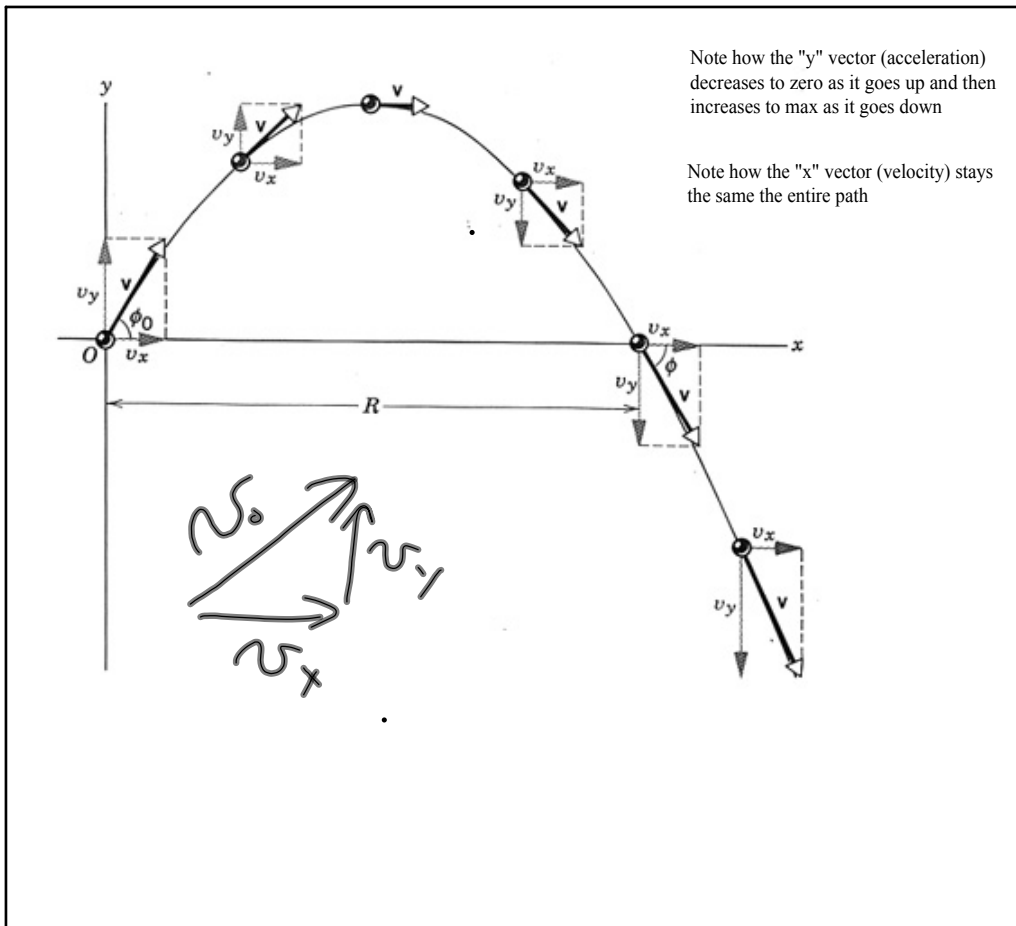
Nov 14-10:36 AM



Nov 16-8:49 AM



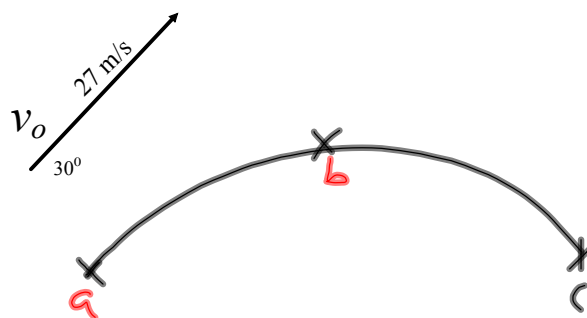
Nov 16-8:50 AM



Dec 4-7:48 AM

A 755 g soccer ball is kicked and leaves the foot at 27.0 m/s at 30.0° from the horizontal. a) How long is it in the air? b) How far does it go? c) How high does it go?

- $m = 0.755 \text{ kg}$
 $a_y = -9.81 \text{ m/s}^2$
 $a_x = 0$
 $v_o = 27.0 \text{ m/s}$
 $\theta = 30.0^\circ$
 a) $t = ?$
 b) $d_x = ?$
 c) $d_y = ?$



Dec 4-7:57 AM

$v_o = 27.0 \text{ m/s}$
 $\theta = 30.0^\circ$
 a) $t = ?$
 b) $d_x = ?$
 c) $d_y = ?$

1) data
 2) diagram
 3) ID planes of motion
 4) ID forces acting on system (object)
 4) ID motion (s) involved with each force

time in air is from **A** to **C**

how high is **A** to **B**, \therefore 1/2 the time

$v_x = 23.4 \text{ m/s}$
 $d_x = ?$
 $v_x = d_x/t$
 $d_x = vt$
 $d_x = 23.4 \text{ m/s} (t)$
 $d_x = 23.4 \text{ m/s} \times 2.75 \text{ s}$
 $d_x = 64.4 \text{ m}$

$v_y = \sin 30.0^\circ (27.0 \text{ m/s}) = 13.5 \text{ m/s}$
 $v_x = \cos 30.0^\circ (27.0 \text{ m/s}) = 23.4 \text{ m/s}$

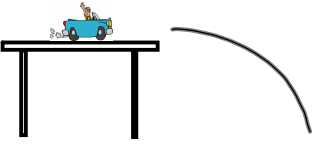
II (x)	I (y)
no force $\Sigma F = 0$	gravity $\therefore \Sigma F = ma$
$\therefore v_c$	$\therefore a$
$v_x = 23.4 \text{ m/s}$	$v_{y1} = 13.5 \text{ m/s}$
$d_x = ?$	$a = g = -9.81 \text{ m/s}^2$
$v_x = d_x/t$	$v_{y2} = 0 \text{ (top)}$
$d_x = vt$	$v_{y3} = -13.5 \text{ m/s (end)}$
$d_x = 23.4 \text{ m/s} (t)$	could solve for "t" or "d"
$d_x = 23.4 \text{ m/s} \times 2.75 \text{ s}$	$d_y = ?$
$d_x = 64.4 \text{ m}$	$t = ?$
	$t_1 = v_{y3} - v_{y1}/a$
	$t = -13.5 \text{ m/s} - (13.5 \text{ m/s})/(-9.81 \text{ m/s}^2)$
	$t = 2.75 \text{ s}$
	$d_y = v_{y2}^2 - v_{y1}^2/2a$
	$d_y = [0 - (13.5 \text{ m/s})^2]/[2(-9.81 \text{ m/s}^2)]$
	$d_y = 9.30 \text{ m}$

Dec 4-7:57 AM

$v_{ox} = 1.3 \text{ m/s}$
 b) $d_y = 92 \text{ cm}$
 c) $d_x = ?$

Dec 15-6:45 AM

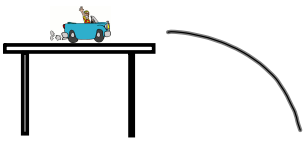
$v_{ox} = 1.3 \text{ m/s}$
 b) $d_y = 92 \text{ cm}$
 c) $d_x = ?$



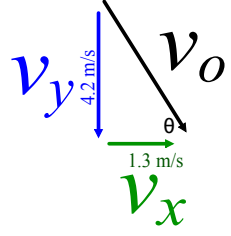
X	Y
<i>const. vel</i>	<i>accel</i>
$\Sigma F = 0$	<i>force of gravity</i> $\therefore \Sigma F = ma$
$v_{ox} = 1.3 \text{ m/s}$	$d_y = 92 \text{ cm}$
$d_x = ?$	$a_y = -9.8 \text{ m/s}^2$
$v_c = d_x/t$	$t = ?$
$d_x = v_c(t)$	$d = 1/2 at^2$
$d_x = 1.3 \text{ m/s}(.43 \text{ s})$	$t = \sqrt{2d/a}$
$d_x = .56 \text{ m}$	$t = \sqrt{[2(.92\text{m})]/-9.8 \text{ m/s}^2}$
	$t = .43 \text{ s}$

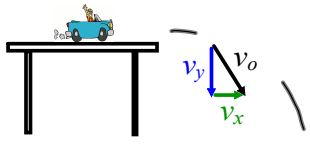
Dec 15-6:48 AM

$v_{ox} = 1.3 \text{ m/s}$
 b) $d_y = 92 \text{ cm}$
 c) $d_x = ?$



What angle did the little car hit the ground at? what velocity?





$v_{y1} = 0$
 $v_{y2} = ?$
 $a = -9.8 \text{ m/s}^2$
 $d = -0.92 \text{ m}$

$\tan \theta = (4.2 \text{ m/s})/1.3 \text{ m/s}$
 $\theta = 73^\circ \text{ above the horizontal}$

$v_o = \sqrt{(4.2 \text{ m/s})^2 + (1.3 \text{ m/s})^2}$
 $v_o = 4.4 \text{ m/s at } 73^\circ \text{ above the horizontal}$

$v_{y2} = \sqrt{2(-9.8 \text{ m/s}^2)(-0.92 \text{ m})}$
 $v_{y2} = -4.2 \text{ m/s}$

Jan 3-6:32 AM



Junior's car is traveling at 65 mph and he drops a test object from 1.7 m above the ground. How far from the drop point does the test object hit the ground?

$$v_x = 65 \text{ mph}$$

$$\quad \quad \quad \hookrightarrow 29 \text{ m/s}$$

$$d_y = -1.7 \text{ m}$$

$$d_x ?$$

Jan 3-7:37 AM



$$v_x = 65 \text{ mph}$$

$$\quad \quad \quad \hookrightarrow 29 \text{ m/s}$$

$$d_y = -1.7 \text{ m}$$

$$d_x ?$$

Junior's car is traveling at 65 mph and he drops a test object from 1.7 m above the ground. How far from the drop point does the test object hit the ground?

X

Y

const. vel

accel

$$\Sigma F = 0$$

force of gravity $\therefore \Sigma F = ma$

$$v_{ox} = 1.3 \text{ m/s}$$

$$d_y = -1.7 \text{ m}$$

$$a_y = -9.8 \text{ m/s}^2$$

$$d_x = ?$$

$$t = ?$$

$$v_c = d_x/t$$

$$d = 1/2 at^2$$

$$d_x = v_c(t)$$

$$t = \sqrt{2d/a}$$

$$d_x = 29 \text{ m/s} (.59 \text{ s})$$

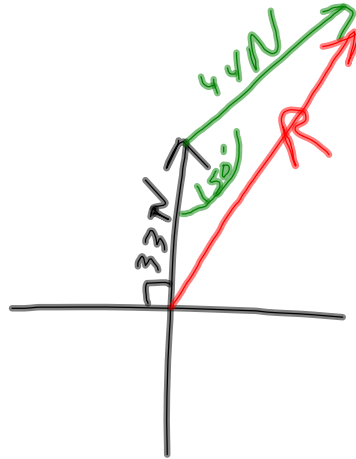
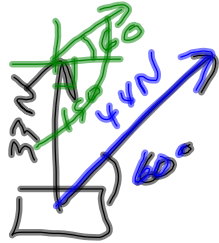
$$t = \sqrt{[2(-1.7\text{m})]/-9.8 \text{ m/s}^2}$$

$$d_x = 17 \text{ m}$$

$$t = .59 \text{ s}$$

Nov 21-6:52 AM

30



Equilibrium

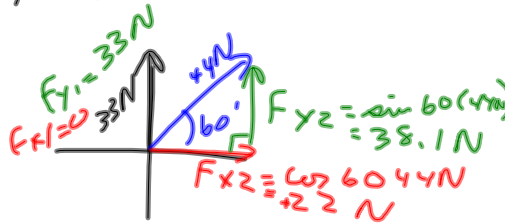
* $\Sigma F = 0$

$R = -E$

graphically,
Law of Sines/Cosines
 $\Sigma F_x; \Sigma F_y$

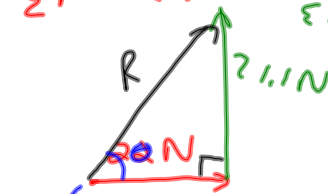
Dec 8 - 10:33 AM

$\Sigma F_x; \Sigma F_y$



$\Sigma F_x: F_{x1} = 0$
 $F_{x2} = +22$
 $\Sigma F_x = 22 N$

$\Sigma F_y = F_{y1} = +33 N$
 $F_{y2} = +38.1 N$
 $\Sigma F_y = 71.1 N$



$R = \sqrt{(22 N)^2 + (71.1 N)^2}$
 $R = 74.4 N$ at 73°
 $E = 74.4 N$ at 253°

73°
 $+ 180^\circ =$
 253°

Dec 8 - 10:40 AM

$a = \sqrt{b^2 + c^2 - 2bc \cos A}$

$$R = \sqrt{(33N)^2 + (44N)^2 - 2(33N)(44N)\cos 150}$$

$$R = 74N \text{ at } 73^\circ$$

$E = -R$ $aE = 74N \text{ at } 253^\circ$ $\frac{180}{73} = \frac{253}{17}$

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

$$\frac{74N}{\sin 150} = \frac{44N}{\sin C}$$

$$C = 17^\circ$$

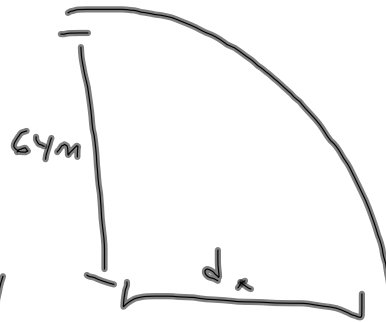
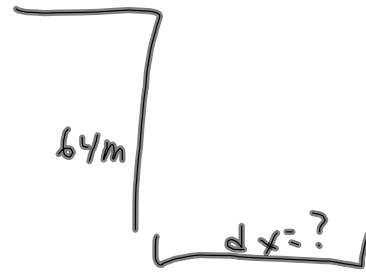
Dec 8 - 12:39 PM

(31)

Dec 8 - 12:34 PM

39

$v_x = 8 \text{ m/s}$



$\Sigma F = 0$
 no v , no F

$\frac{y}{t} = ?$
 $d_y = -64 \text{ m}$
 $a = -9.8 \text{ m/s}^2$

v_c
 $v = d/t$ $d = \frac{1}{2}at^2$ $t = \sqrt{2y/a}$

$v_x = \frac{d_x}{t}$ $d_x = v_x t = 8 \text{ m/s}(t)$

Dec 8 - 12:30 PM



$v_c = v = d/t$

x

y

	v	a	t
	d	a	t
	v	a	d
	d	v	t

Dec 8 - 1:29 PM