

Friction:

- 1) caused by the interaction of 2 + objects
- 2) opposite (opposes) motion
- 3) Types- Kinetic, static, sliding, rolling
- 4) size determined by:
 - nature of surfaces
 - force pushing surfaces together

frictional characteristic of the surfaces
"coefficient of friction"

$$F_f = \mu F_N$$

force of friction

Normal Force
force pushing surfaces together
⊥ to surface

" μ " is the "coefficient of friction" and is the frictional property of the two surfaces in contact. Each pair of surfaces has its own unique value of μ . Note that μ is a ratio of forces, and therefore a pure number.

$$\mu = F_f / F_N$$

F_f is **parallel** to surface F_N is **perpendicular** to surface

plane of motion!

The diagram illustrates the relationship between the coefficient of friction μ and the forces F_f and F_N . The equation $\mu = F_f / F_N$ is shown at the top. Below it, two arrows point from the text " F_f is parallel to surface" and " F_N is perpendicular to surface" to the F_f and F_N terms in the equation, respectively. A green arrow points from the text "plane of motion!" to both the F_f and F_N terms, indicating that both forces lie in the plane of motion.

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

1) data?

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

Plane of motion: Motion is along the horizontal

With the question of *Type Motion* and *Type force* you have to consider planes **parallel** and **perpendicular to motion**.

2) Type motion?

3) Type force?

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

horizontal (x)
parallel

$$v_c \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$

vertical (y)
perpendicular

$$\text{rest} \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$

as the box slides across the floor it is not moving up or down, therefore it is at rest in the "y" (perpendicular) axis

4) picture? (diagram)

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

horizontal (x)

parallel

$$v_c \therefore 1^{\text{st}} \text{ Law}$$

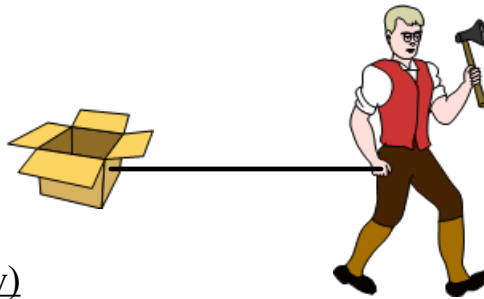
$$\Sigma F = 0$$

vertical (y)

perpendicular

$$\text{rest} \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$



5) force diagram

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

horizontal (x)

parallel

$$v_c \therefore 1^{\text{st}} \text{ Law}$$

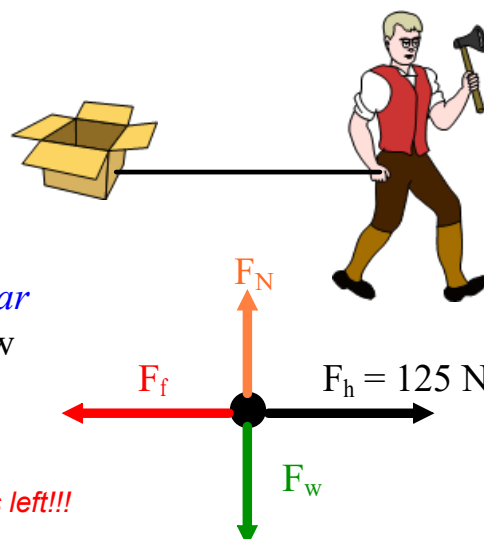
$$\Sigma F = 0$$

vertical (y)

perpendicular

$$\text{rest} \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$



the box is sliding right, there F_f is left!!!

6) Determine any forces you don't know

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$
$f_h = 125 \text{ N}$
v_c
$\mu?$
horizontal (x) vertical (y)
parallel perpendicular
$v_c \therefore 1^{\text{st}} \text{ Law}$ rest
$\Sigma F = 0$ $\Sigma F = 0$



<p>horizontal (x)</p> <p>$\Sigma F = 0$</p> <p>$F_f + F_h = 0$</p> <p>$F_f = -F_h$</p> <p>$F_f = -(125 \text{ N})$</p> <p>$F_f = -125 \text{ N}$</p>	<p>vertical (y)</p> <p>$\Sigma F = 0$</p> <p>$F_w + F_N = 0$</p> <p>$F_N = -F_w$</p> <p>$F_N = -(mg)$</p> <p>$F_N = -(-245 \text{ N})$</p> <p>$F_N = (245 \text{ N})$</p>		<p>$F_w = mg$</p> <p>$F_w = 25. \text{kg} (-9.8 \text{ m/s}^2)$</p> <p>$F_w = -245 \text{ N}$</p>
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7) Find unknown

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$
$f_h = 125 \text{ N}$
v_c
$\mu?$
horizontal (x) vertical (y)
parallel perpendicular
$v_c \therefore 1^{\text{st}} \text{ Law}$ rest
$\Sigma F = 0$ $\Sigma F = 0$



<p>horizontal (x)</p> <p>$\Sigma F = 0$</p> <p>$F_f + F_h = 0$</p> <p>$F_f = -F_h$</p> <p>$F_f = -(125 \text{ N})$</p> <p>$F_f = -125 \text{ N}$</p>	<p>vertical (y)</p> <p>$\Sigma F = 0$</p> <p>$F_w + F_N = 0$</p> <p>$F_N = -F_w$</p> <p>$F_N = -(mg)$</p> <p>$F_N = -(-245 \text{ N})$</p> <p>$F_N = (245 \text{ N})$</p>		<p>$F_w = mg$</p> <p>$F_w = 25 \text{ kg} (-9.8 \text{ m/s}^2)$</p> <p>$F_w = -245 \text{ N}$</p>
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$\mu = F_f/F_N$

$\mu = -125 \text{ N}/245 \text{ N}$

$\mu = 0.510$

The "-" in μ is meaningless because it is a vector direction and μ is not a vector- it is a pure number (ratio of forces), therefore it is dropped

7) Find unknown

You pull a 25.0 kg box across a *waxed* floor with an acceleration of 2.50 m/s^2 with a horizontal force of 125 N. What is μ ?

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$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$a = 2.50 \text{ m/s}^2$$

μ ?

horizontal

$a \therefore 2^{\text{nd}}$ Law

$$\Sigma F = ma$$

vertical

rest

$$\Sigma F = 0$$

$$F_f + F_h = ma$$

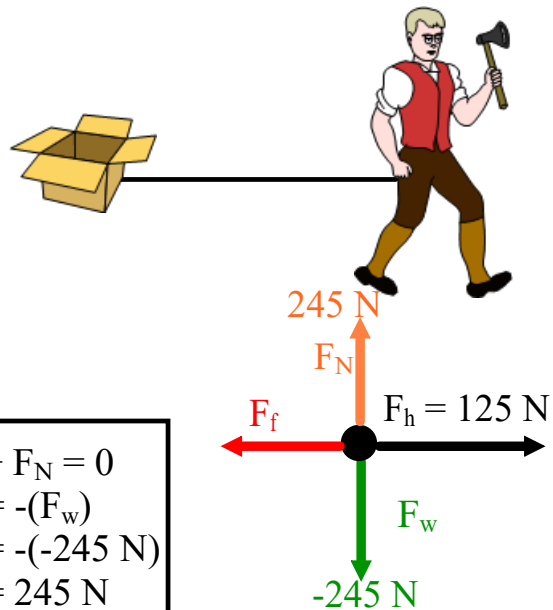
$$F_f = ma - F_h$$

$$F_f = 25.0 \text{ kg}(2.50 \text{ m/s}^2) - (125 \text{ N})$$

$$F_f = 62.5 \text{ N} - (125 \text{ N})$$

$$F_f = -62.5 \text{ N}$$

$$\begin{aligned} F_w + F_N &= 0 \\ F_N &= -(F_w) \\ F_N &= -(-245 \text{ N}) \\ F_N &= 245 \text{ N} \end{aligned}$$



You pull a 25.0 kg box across a *waxed* floor with an acceleration of 2.50 m/s^2 with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

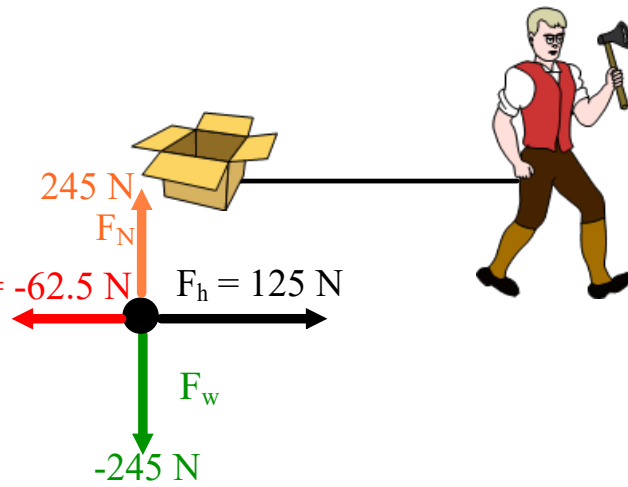
$$f_h = 125 \text{ N}$$

$$a = 2.50 \text{ m/s}^2$$

$$\mu?$$

horizontal
 $a \therefore 2^{\text{nd}} \text{ Law}$
 $\Sigma F = ma$

vertical
 rest
 $\Sigma F = 0$

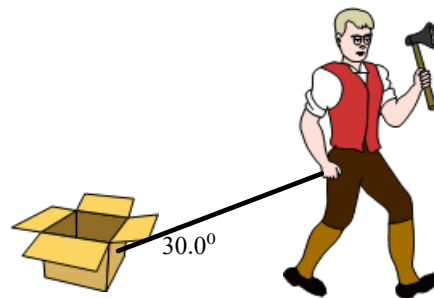


$$\mu = F_f / F_N$$

$$\mu = -62.5 \text{ N} / 245 \text{ N}$$

$$\mu = 0.255$$

You pull a 25.0 kg box across a floor at a constant velocity with a force of 125 N directed 30.0° above the horizontal. What is μ ?



You pull a 25.0 kg box across a floor at a constant velocity with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$

$f_a = 125 \text{ N at } 30.0^\circ$

v_c

$\mu?$

horizontal

parallel

$v_c \therefore 1^{\text{st}} \text{ Law}$

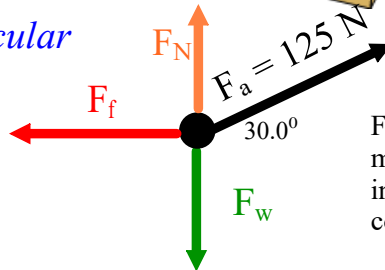
$\Sigma F = 0$

vertical

perpendicular

rest

$\Sigma F = 0$



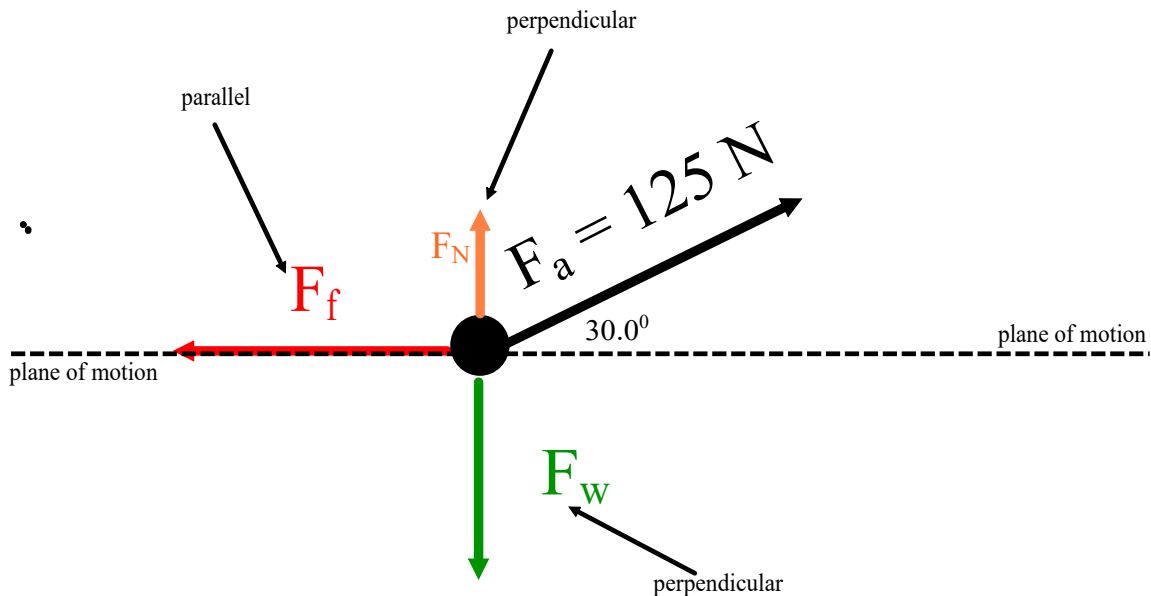
F_a isn't parallel or perpendicular to motion, it's both, so break it down into its parallel and perpendicular components.

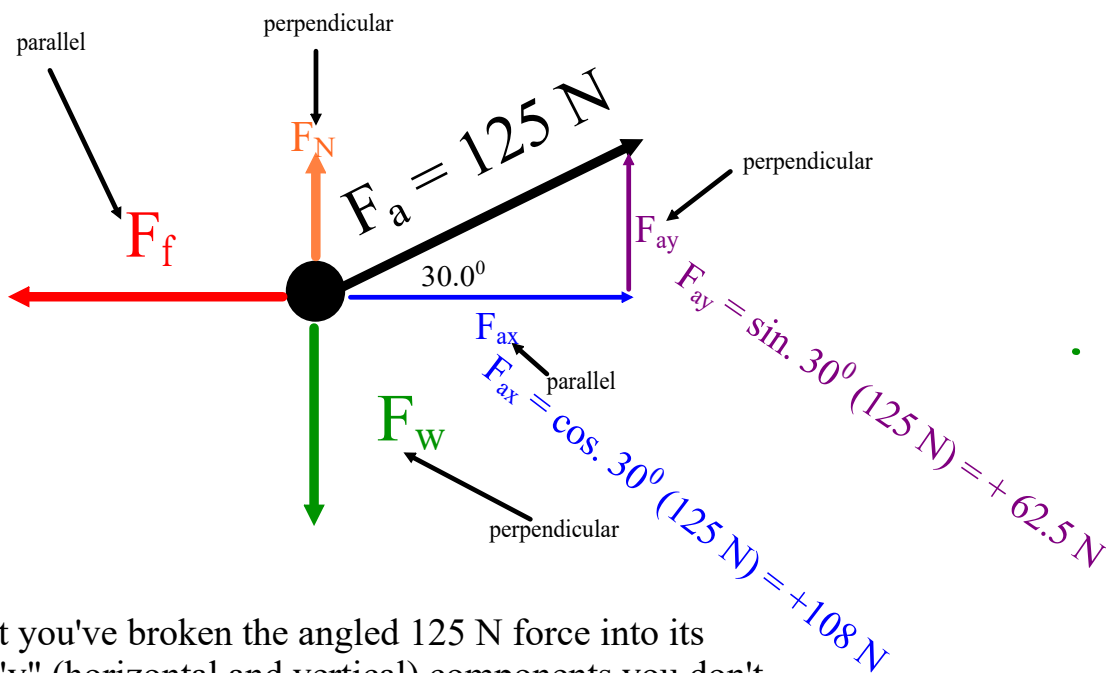
parallel to motion

$\mu = F_f / F_N$

perpendicular to motion

break down (resolve) all forces into their parallel and perpendicular components!!!!





Now that you've broken the angled 125 N force into its "x" and "y" (horizontal and vertical) components you don't use it (the 125 N force), you just use its components!!!

You pull a 25.0 kg box across a floor at a constant velocity with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$

$F_a = 125 \text{ N at } 30.0^\circ$

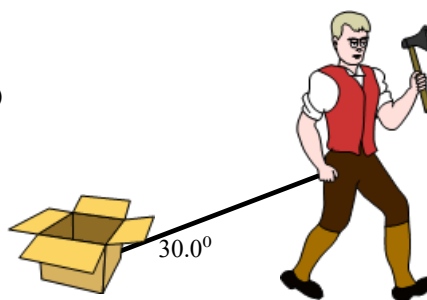
v_c

$\mu?$

$F_w = mg$

$F_w = 25 \text{ kg} (-9.8 \text{ m/s}^2)$

$F_w = -245 \text{ N}$



horizontal

parallel

$v_c \therefore 1^{\text{st}} \text{ Law}$

$\Sigma F = 0$

$\Sigma F = 0$

$F_f + F_{ax} = 0$

$F_f = -F_{ax}$

$F_f = -(108\text{N})$

$F_f = -108 \text{ N}$

vertical

perpendicular

rest

$\Sigma F = 0$

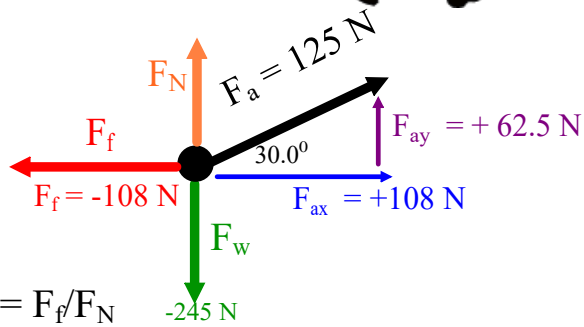
$\Sigma F = 0$

$F_w + F_N + F_{ay} = 0$

$F_N = -F_w - F_{ay}$

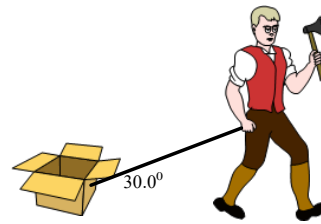
$F_N = -(-245 \text{ N}) - (62.5\text{N})$

$F_N = 182.5 \text{ N}$



$\mu = F_f/F_N$
 $\mu = -108 \text{ N}/182.5 \text{ N}$
 $\mu = 0.592$

You pull a 25.0 kg box across a waxed floor with an acceleration of 2.00 m/s² with a force of 125 N directed 30.0° above the horizontal. What is μ ?



You pull a 25.0 kg box across a waxed floor with an acceleration of 2.00 m/s² with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$
 $f_a = 125 \text{ N at } 30.0^\circ$
 acceleration

$F_w = mg$
 $F_w = 25 \text{ kg } (-9.8 \text{ m/s}^2)$
 $F_w = -245 \text{ N}$

$\mu?$

horizontal

parallel

$a \therefore 2^{\text{nd}}$ Law

$\Sigma F = ma$

$F_f + F_{ax} = ma$

$F_f = ma - F_{ax}$

$F_f = 25.0 \text{ kg}(2.00 \text{ m/s}^2) - (108\text{N})$

$F_f = -58 \text{ N}$

vertical

perpendicular

rest

$\Sigma F = 0$

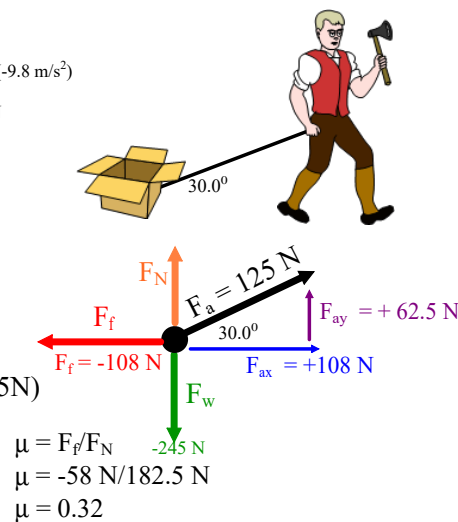
$\Sigma F = 0$

$F_w + F_N + F_{ay} = 0$

$F_N = -F_w - F_{ay}$

$F_N = -(-245 \text{ N}) - (62.5\text{N})$

$F_N = 182.5 \text{ N}$



1) You pull a 25.0 kg box across a waxed floor with an acceleration of 2.00 m/s² with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$

$f_a = 125 \text{ N at } 30.0^\circ$

acceleration

$\mu?$

horizontal

parallel

$a \therefore 2^{\text{nd}}$ Law

$\Sigma F = ma$

vertical

perpendicular

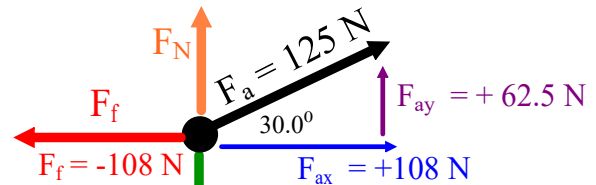
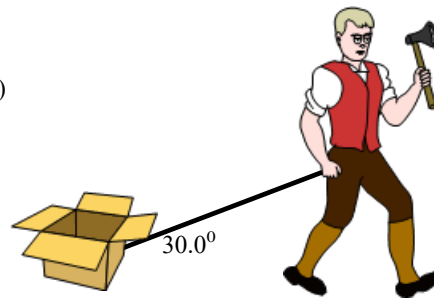
rest

$\Sigma F = 0$

$F_w = mg$

$F_w = 25 \text{ kg} (-9.8 \text{ m/s}^2)$

$F_w = -245 \text{ N}$



$F_f + F_{ax} = ma$

$F_f = ma - F_{ax}$

$\Sigma F = 0$

$F_w + F_N + F_{ay} = 0$

$F_N = -F_w - F_{ay}$

$F_N = -(-245 \text{ N}) - (62.5 \text{ N})$

$F_N = 182.5 \text{ N}$

$\mu = F_f / F_N$

$\mu = -58 \text{ N} / 182.5 \text{ N}$

$\mu = 0.32$

$F_f = 25.0 \text{ kg}(2.00 \text{ m/s}^2) - (108 \text{ N})$

$F_f = -58 \text{ N}$