

Friction:

- 1) caused by the interaction of 2 + objects
- 2) opposite (opposes) motion
- 3) Types- Kinetic, static, sliding, rolling
- 4) size determined by:
 - nature of surfaces
 - force pushing surfaces together

frictional characteristic of the surfaces
"coefficient of friction"

$$F_f = \mu F_N$$

force of friction

Normal Force
force pushing surfaces together
⊥ to surface

The diagram shows the equation $F_f = \mu F_N$ with three arrows pointing to its components. An arrow points from the text 'frictional characteristic of the surfaces "coefficient of friction"' to the Greek letter mu (μ). Another arrow points from the text 'force of friction' to the F_f term. A third arrow points from the text 'Normal Force force pushing surfaces together ⊥ to surface' to the F_N term.

" μ " is the "coefficient of friction" and is the frictional property of the two surfaces in contact. Each pair of surfaces has its own unique value of μ . Note that μ is a ratio of forces, and therefore a pure number.

$$\mu = F_f / F_N$$

F_f is parallel to surface F_N is perpendicular to surface

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

1) data?

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

Plane of motion: Motion is along the horizontal

With the question of *Type Motion* and *Type force* you have to consider planes parallel and perpendicular to motion.

2) Type motion?

3) Type force?

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

horizontal (x)
parallel

$$v_c \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$

vertical (y)
perpendicular

$$\text{rest} \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$

as the box slides across the floor it is not moving up or down, therefore it is at rest in the "y" (perpendicular) axis

4) picture? (diagram)

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

horizontal (x)

parallel

$$v_c \therefore 1^{\text{st}} \text{ Law}$$

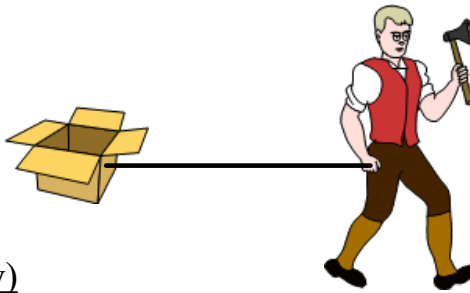
$$\Sigma F = 0$$

vertical (y)

perpendicular

$$\text{rest} \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$



5) force diagram

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$v_c$$

$$\mu?$$

horizontal (x)

parallel

$$v_c \therefore 1^{\text{st}} \text{ Law}$$

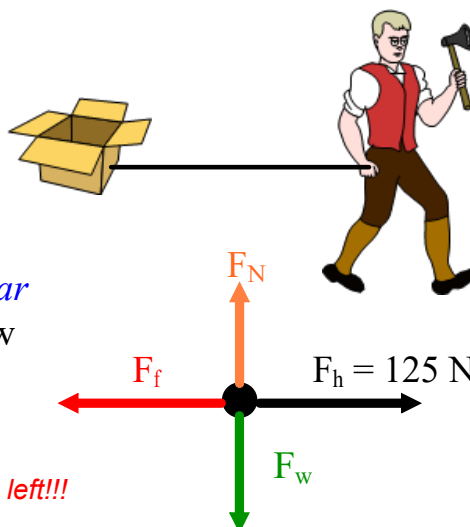
$$\Sigma F = 0$$

vertical (y)

perpendicular

$$\text{rest} \therefore 1^{\text{st}} \text{ Law}$$

$$\Sigma F = 0$$



the box is sliding right, there F_f is left!!!

6) Determine any forces you don't know

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?



$m_{\text{box}} = 25 \text{ kg}$
$f_h = 125 \text{ N}$
v_c
$\mu?$
horizontal (x) vertical (y)
parallel perpendicular
$v_c \therefore 1^{\text{st}} \text{ Law}$ rest
$\Sigma F = 0$ $\Sigma F = 0$

horizontal (x)

$$\Sigma F = 0$$

$$F_f + F_h = 0$$

$$F_f = -F_h$$

$$F_f = -(125 \text{ N})$$

$$F_f = -125 \text{ N}$$

vertical (y)

$$\Sigma F = 0$$

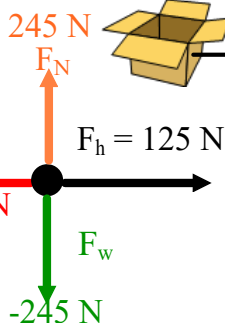
$$F_w + F_N = 0$$

$$F_N = -F_w$$

$$F_N = -(mg)$$

$$F_N = -(-245 \text{ N})$$

$$F_N = (245 \text{ N})$$



$$F_w = mg$$

$$F_w = 25 \text{ kg} (-9.8 \text{ m/s}^2)$$

$$F_w = -245 \text{ N}$$

7) Find unknown

You pull a 25.0 kg box across a floor at a constant velocity with a horizontal force of 125 N. What is μ ?



$m_{\text{box}} = 25 \text{ kg}$
$f_h = 125 \text{ N}$
v_c
$\mu?$
horizontal (x) vertical (y)
parallel perpendicular
$v_c \therefore 1^{\text{st}} \text{ Law}$ rest
$\Sigma F = 0$ $\Sigma F = 0$

horizontal (x)

$$\Sigma F = 0$$

$$F_f + F_h = 0$$

$$F_f = -F_h$$

$$F_f = -(125 \text{ N})$$

$$F_f = -125 \text{ N}$$

vertical (y)

$$\Sigma F = 0$$

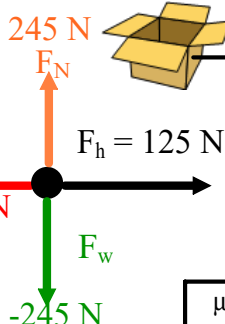
$$F_w + F_N = 0$$

$$F_N = -F_w$$

$$F_N = -(mg)$$

$$F_N = -(-245 \text{ N})$$

$$F_N = (245 \text{ N})$$



$$F_w = mg$$

$$F_w = 25 \text{ kg} (-9.8 \text{ m/s}^2)$$

$$F_w = -245 \text{ N}$$

$$\mu = F_f/F_N$$

$$\mu = -125 \text{ N}/245 \text{ N}$$

$$\mu = 0.510$$

The "-" in μ is meaningless because it is a vector direction and μ is not a vector- it is a pure number, therefore it is dropped

7) Find unknown

You pull a 25.0 kg box across a *waxed* floor with an acceleration of 2.50 m/s^2 with a horizontal force of 125 N. What is μ ?

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$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$a = 2.50 \text{ m/s}^2$$

$$\mu?$$

horizontal
 $a \therefore 2^{\text{nd}} \text{ Law}$
 $\Sigma F = ma$

vertical
 rest
 $\Sigma F = 0$

$$F_f + F_h = ma$$

$$F_f = ma - F_h$$

$$F_f = 25.0 \text{ kg}(2.50 \text{ m/s}^2) - (125 \text{ N})$$

$$F_f = 62.5 \text{ N} - (125 \text{ N})$$

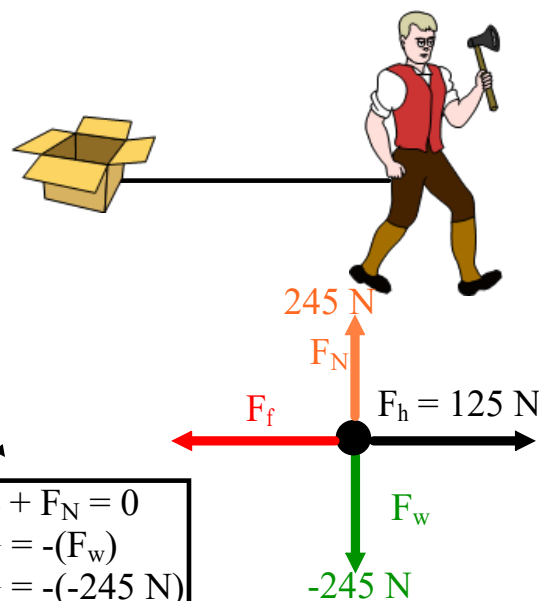
$$F_f = -62.5 \text{ N}$$

$$F_w + F_N = 0$$

$$F_N = -(F_w)$$

$$F_N = -(-245 \text{ N})$$

$$F_N = 245 \text{ N}$$



You pull a 25.0 kg box across a *waxed* floor with an acceleration of 2.50 m/s^2 with a horizontal force of 125 N. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$f_h = 125 \text{ N}$$

$$a = 2.50 \text{ m/s}^2$$

μ ?

horizontal

$a \therefore 2^{\text{nd}}$ Law

$$\Sigma F = ma$$

vertical

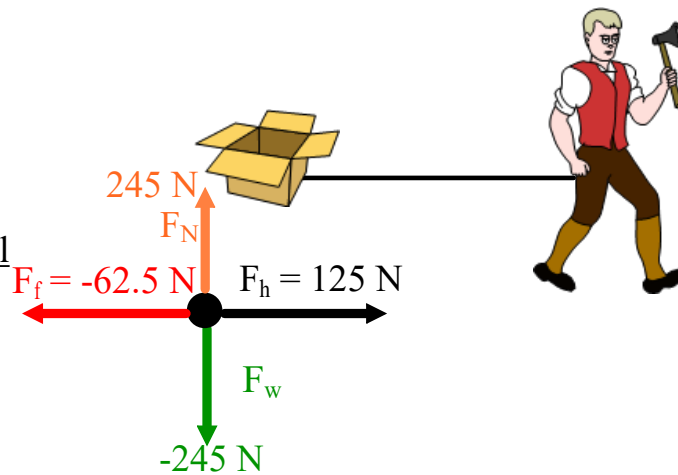
rest

$$\Sigma F = 0$$

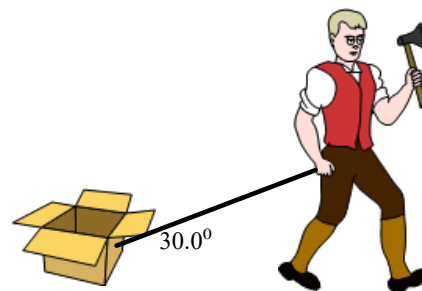
$$\mu = F_f / F_N$$

$$\mu = -62.5 \text{ N} / 245 \text{ N}$$

$$\mu = 0.255$$



You pull a 25.0 kg box across a floor at a constant velocity with a force of 125 N directed 30.0° above the horizontal. What is μ ?



You pull a 25.0 kg box across a floor at a constant velocity with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$
 $f_a = 125 \text{ N at } 30.0^\circ$

v_c

$\mu?$

horizontal

parallel

$v_c \therefore 1^{\text{st}} \text{ Law}$

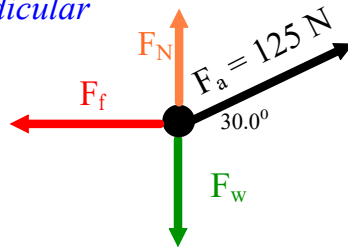
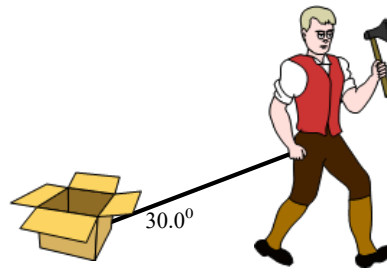
$\Sigma F = 0$

vertical

perpendicular

rest

$\Sigma F = 0$



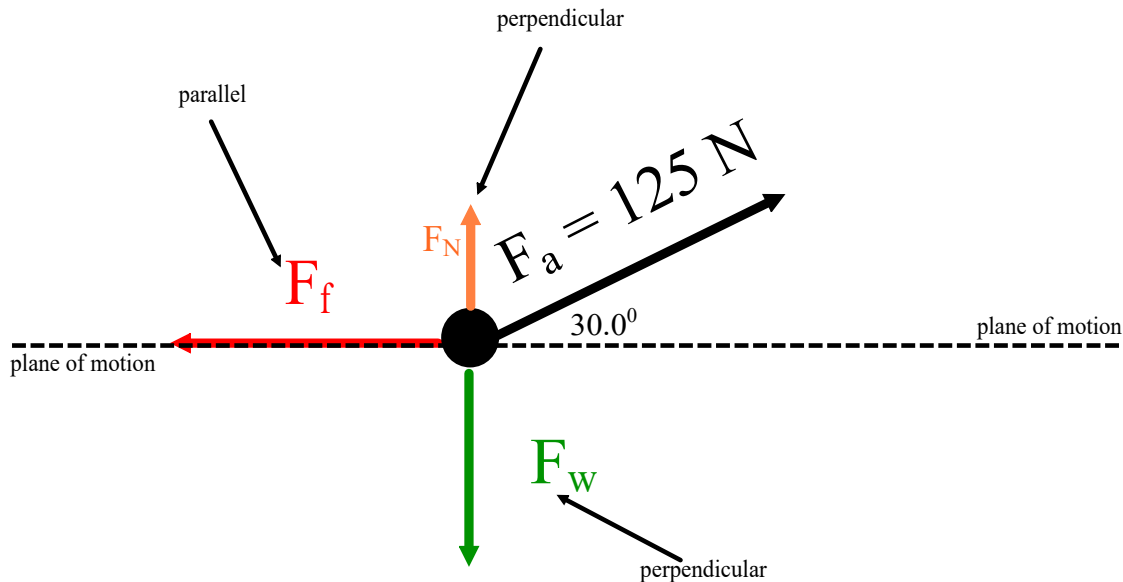
F_a isn't parallel or perpendicular to motion, it's both, so break it down into its parallel and perpendicular components.

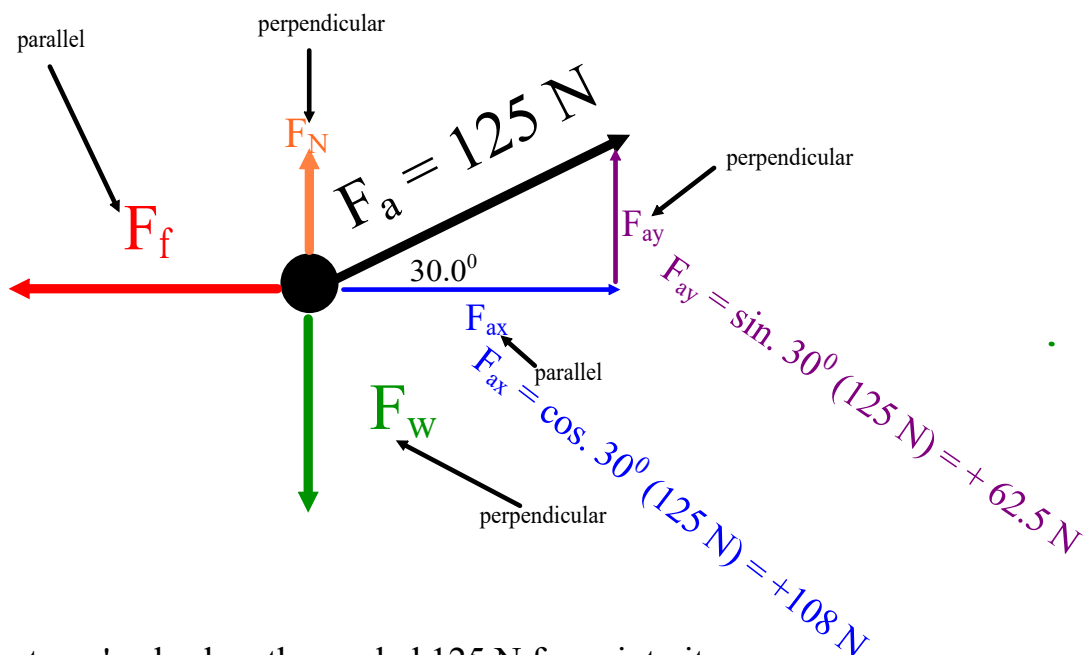
parallel to motion

$\mu = F_f / F_N$

perpendicular to motion

break down (resolve) all forces into their parallel and perpendicular components!!!!



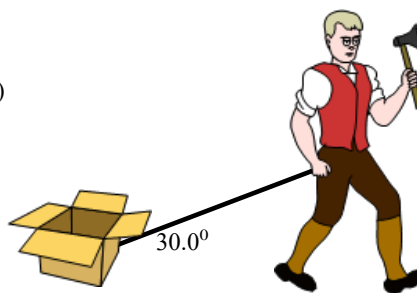


Now that you've broken the angled 125 N force into its "x" and "y" (horizontal and vertical) components you don't use it (the 125 N force), you just use its components!!!

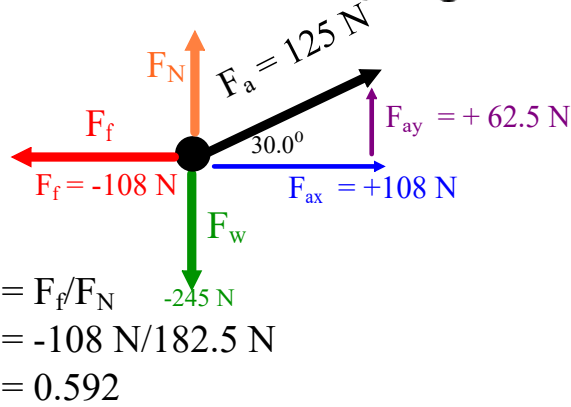
You pull a 25.0 kg box across a floor at a constant velocity with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$m_{\text{box}} = 25 \text{ kg}$
 $F_a = 125 \text{ N at } 30.0^\circ$
 v_c
 $\mu?$

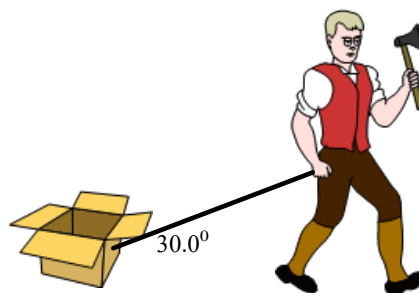
$F_w = mg$
 $F_w = 25 \text{ kg} (-9.8 \text{ m/s}^2)$
 $F_w = -245 \text{ N}$



<u>horizontal</u>	<u>vertical</u>
<i>parallel</i>	<i>perpendicular</i>
$v_c \therefore 1^{\text{st}} \text{ Law}$	rest
$\Sigma F = 0$	$\Sigma F = 0$
$\Sigma F = 0$	$\Sigma F = 0$
$F_f + F_{ax} = 0$	$F_w + F_N + F_{ay} = 0$
$F_f = -F_{ax}$	$F_N = -F_w - F_{ay}$
$F_f = -(108\text{N})$	$F_N = -(-245 \text{ N}) - (62.5\text{N})$
$F_f = -108 \text{ N}$	$F_N = 182.5 \text{ N}$



You pull a 25.0 kg box across a waxed floor with an acceleration of 2.00 m/s^2 with a force of 125 N directed 30.0° above the horizontal. What is μ ?



You pull a 25.0 kg box across a waxed floor with an acceleration of 2.00 m/s^2 with a force of 125 N directed 30.0° above the horizontal. What is μ ?

$$m_{\text{box}} = 25 \text{ kg}$$

$$F_a = 125 \text{ N at } 30.0^\circ$$

acceleration

μ ?

horizontal

parallel

$a \therefore 2^{\text{nd}}$ Law

$$\Sigma F = ma$$

$$F_f + F_{ax} = ma$$

$$F_f = ma - F_{ax}$$

$$F_f = 25.0 \text{ kg}(2.00 \text{ m/s}^2) - (108\text{N})$$

$$F_f = -58 \text{ N}$$

$$F_w = mg$$

$$F_w = 25 \text{ kg}(-9.8 \text{ m/s}^2)$$

$$F_w = -245 \text{ N}$$

vertical

perpendicular

rest

$$\Sigma F = 0$$

$$\Sigma F = 0$$

$$F_w + F_N + F_{ay} = 0$$

$$F_N = -F_w - F_{ay}$$

$$F_N = -(-245 \text{ N}) - (62.5\text{N})$$

$$F_N = 182.5 \text{ N}$$

