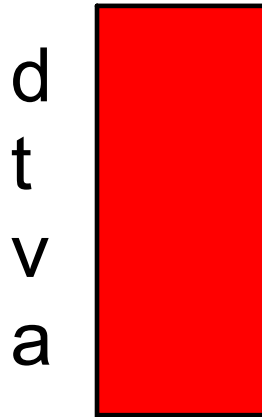


What are the variables (characteristics you can measure) of an object in motion?



$v_c = d/t$

---

$v_c$  constant velocity

varying velocity

$\bar{v} = \frac{\Delta d}{t}$

$v_v$  (varying/acceleration) by definition  $\bar{v} = \frac{v_1 + v_2}{t}$

$\frac{v_1 + v_2}{2} = d/t$  multiply by "t"

$d = \left( \frac{v_1 + v_2}{2} \right) t$   $\bar{v} = \frac{v_1 + v_2}{2}$

or,

$d = \bar{v} t$

*(Note: In the original image, 'dvt' is circled in red and the equation  $d = \left( \frac{v_1 + v_2}{2} \right) t$  is circled in green.)*

You go from 15 m/s to 25 m/s in 2.0 s.  
How far did you go?

***What are the steps in solving this problem??????***

You go from 15 m/s to 25 m/s in 2.0 s.  
How far did you go?

- 1) list data- do any conversions if needed
  - 1a) draw diagram/picture if needed
- 2) "TM" type motion ...  
list base formula ... simplify...
- 3) isolate variable
- 4) plug in measurements  
*-estimate*
- 5) solve equation  
*-reasonableness*
- 6) do unit analysis

$$d = \left( \frac{v_1 + v_2}{2} \right) t$$

You go from 15 m/s to 25 m/s in 2.0 s.  
How far did you go?

①  $v_1 = 15 \text{ m/s}$       ②  $d = v t$

$v_2 = 25 \text{ m/s}$

$t = 2.0 \text{ s}$   
 $d = ?$

$$d = \left( \frac{v_1 + v_2}{2} \right) t$$

7 m       $d = \left( \frac{15 \text{ m/s} + 25 \text{ m/s}}{2} \right) 2.0 \text{ s}$

$$d = 40 \text{ m}$$

$(\text{m/s} + \text{m/s}) \times 2$   
 $\text{m/s} \times 2$   
 $\text{m}$

by definition

$$a = \frac{\Delta v}{t}$$

$$\begin{aligned} \Delta v &= v_2 - v_1 \\ &= v_f - v_i \\ &= v - v_0 \end{aligned}$$

$$a = \frac{v_2 - v_1}{t}$$

multiply by "t" and add  $v_1$

$$v_2 = v_1 + a t$$

$$v a t$$

You are traveling at 15 m/s and  
accelerate at  $2.0 \text{ m/s}^2$  for 3.0 s.  
What is your ending velocity?

$$\text{vat } v_2 = v_1 + at$$

You are traveling at 15 m/s and  
accelerate at  $2.0 \text{ m/s}^2$  for 3.0 s.  
What is your ending velocity?

$$v_1 = 15 \text{ m/s}$$

$$a = 2.0 \text{ m/s}^2$$

$$t = 3.0 \text{ s}$$

$$v_2 = ?$$

$$v_2 = v_1 + at$$

$$v_2 = 15 \text{ m/s} + 2.0 \text{ m/s}^2 (3.0 \text{ s})$$

$$v_2 = 15 \text{ m/s} + 6 \text{ m/s}$$

$$v_2 = 21 \text{ m/s}$$

$$\text{m/s} = \text{m/s} + \text{m/s}^2(\text{s})$$

$$\text{m/s} = \text{m/s} + \text{m/s}$$

$$\text{m/s} = \text{m/s}$$

"dot"

$$d = \left( \frac{v_1 + v_2}{2} \right) t$$

"Nat"

$$v_2 = v_1 + at$$

Simplify

$$d = \left[ \frac{v_1 + (v_1 + at)}{2} \right] t$$

divide through by 2

$$d = \left( \frac{2v_1 + at}{2} \right) t$$

distribute the "t"

$$d = (v_1 + \frac{1}{2}at) t$$

$dat$

$$d_2 = v_1 t + \frac{1}{2}at^2$$

or,

$$\underline{d_2 = d_1 + v_1 t + \frac{1}{2}at^2}$$

How far does a ball fall if it is thrown downward at -15 m/s and strikes the ground 2.0 s later?

How far does a ball fall if it is thrown downward at -15 m/s and strikes the ground 2.0 s later?

$$d = ?$$

$$v_1 = -15 \text{ m/s}$$

$$t = 2.02$$

$$a = -9.8 \text{ m/s}^2 \text{ (understood)}$$

$$d = v_1 t + \frac{1}{2} a t^2$$

$$d = -15 \text{ m/s}(2.02) + \frac{1}{2}(-9.8 \text{ m/s}^2)(2.02)^2$$

$$d = -30 \text{ m} + (-20 \text{ m})$$

$$d = -50 \text{ m}$$

↑  
-down

$$d = v_1 t + \frac{1}{2} a t^2$$

$$m = \frac{m}{s}(\cancel{s}) \quad \frac{m}{s^2}(\cancel{s}^2)$$

↙ ↘  
m + m

d vs t

$$d = \left( \frac{v_1 + v_2}{2} \right) t$$

↑  
v a t  
 $v_2 = v_1 + at$   
 $t = \frac{v_2 - v_1}{a}$

$$d = \left( \frac{v_1 + v_2}{2} \right) \left( \frac{v_2 - v_1}{a} \right)$$

dist

$$d = \frac{v_1 v_2 + v_2 v_2 - v_1 v_1 - v_2 v_1}{2a}$$

$$d = \frac{-\cancel{v_1 v_2} + v_2^2 - v_1^2 - \cancel{v_2 v_1}}{2a}$$

$$d = \frac{-v_2^2 - v_1^2}{2a} \quad v_2 = ?$$

$$v_2^2 = v_1^2 + 2ad$$

x 2a + v<sub>1</sub><sup>2</sup>

v<sub>2</sub> a d

What velocity does a ball hit the ground at if it's thrown downward at -15 m/s from a 25 m cliff?

What velocity does a ball hit the ground at if it's thrown downward at -15 m/s from a 25 m cliff?

$$\begin{aligned}
 v_2 &= ? \\
 v_1 &= -15 \text{ m/s} \\
 d &= -25 \text{ m} \\
 a &= -9.8 \text{ m/s}^2 \\
 \text{"v ad"} \quad v_2^2 &= v_1^2 + 2ad \\
 v_2 &= \sqrt{v_1^2 + 2ad} \\
 v_2 &= \sqrt{(-15 \text{ m/s})^2 + 2(-9.8 \text{ m/s}^2)(-25 \text{ m})} \\
 v_2 &= \sqrt{225 \text{ m}^2/\text{s}^2 + (+490 \text{ m}^2/\text{s}^2)} \\
 v_2 &= \sqrt{715 \text{ m}^2/\text{s}^2} \\
 v_2 &= -27 \text{ m/s}
 \end{aligned}$$

Downward! you have to choose the correct sign

