

Q will either:

Δt or $\Delta \text{state (phase)}$

$\Delta \text{ KE of particles}$

$Q = mc\Delta t$

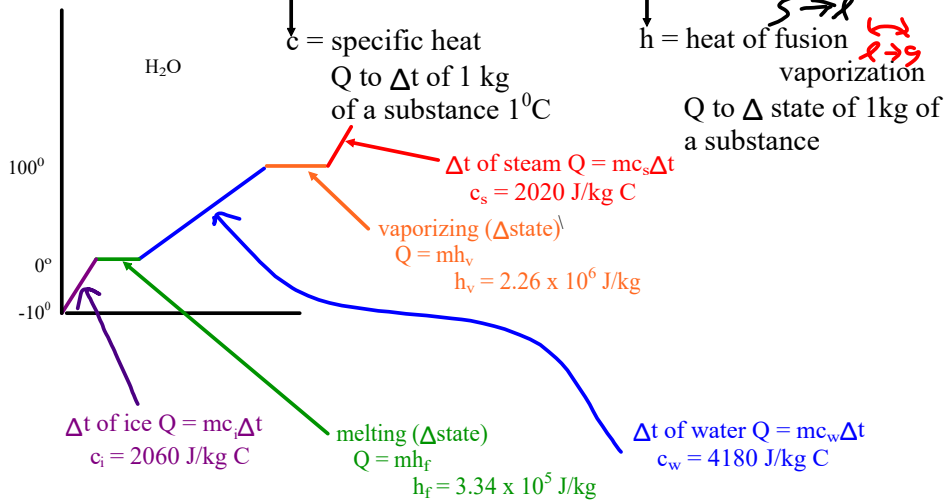
Break bonds

$\Delta \text{ PE}$

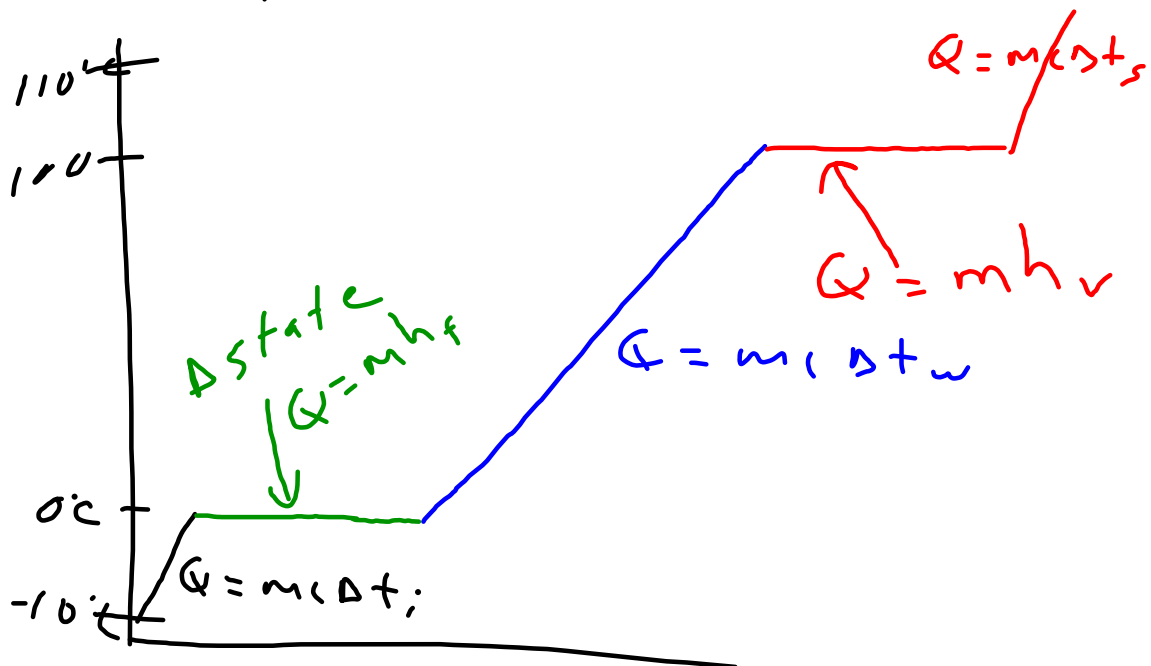
$Q = mh$

$c = \text{specific heat}$
 $Q \text{ to } \Delta t \text{ of } 1 \text{ kg}$
 $\text{of a substance } 1^\circ\text{C}$

$h = \text{heat of fusion}$
 $Q \text{ to } \Delta \text{ state of } 1 \text{ kg}$
 of a substance



H₂O



100.0 g of ice at -10.0°C is placed in 1.00 kg of water at 90.0°C . What is the final temperature of the mixture?

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$m_i = .10\text{ kg}$
 $t_{i_i} = -10^\circ\text{C}$
 $m_w = 1.0\text{ kg}$
 $t_{w_i} = 90^\circ\text{C}$
 $h_f = 3.34 \times 10^5\text{ J/kg}$
 $t_f = ?$

$Q_L + Q_g = 0$
 $mc\Delta t_w + mc\Delta t_i + mh_f + mc\Delta t_{wi} = 0$
 $mc\Delta t_w + mc\Delta t_{wi} = -mc\Delta t_i - mh_f$
expand Δt
 $mct_{fw} - mct_{iw} + mct_{fwi} - mct_{iwi} = -mc\Delta t_i - mh_f$
 $mct_{fw} + mct_{fwi} = -mc\Delta t_i - mh_f + mct_{iw} + mct_{iwi}$
 $t_f(mc_w + mc_{wi}) = -mc\Delta t_i - mh_f + mct_{iw} + mct_{iwi}$
 $t_f = \frac{-mc\Delta t_i - mh_f + mct_{iw} + mct_{iwi}}{(mc_w + mc_{wi})}$

note how the t_f of the ice is different then the t_f of water that came from ice

$t_f = \frac{-.10\text{ kg}(2060\text{ J/kgC})10^\circ\text{C} - .10\text{ kg}(3.34 \times 10^5\text{ J/kg}) + 1\text{ kg}(4180\text{ J/kgC})90.0^\circ\text{C} + .10\text{ kg}(4180\text{ J/kgC})0^\circ\text{C}}{((1\text{ kg}(4180\text{ J/kgC}) + .10\text{ kg}(4180\text{ J/kgC}))}$

$t_f = 74.1^\circ\text{C}$

$Q_L = mc\Delta t_w = 1\text{ kg}(4180\text{ J/kgC})(74.1^\circ - 90^\circ\text{C}) = -66,500\text{ J}$

$Q_g = mc\Delta t_i = .1\text{ kg}(2060\text{ J/kgC})[0 - (-10^\circ\text{C})] = +2060\text{ J}$
 $Q_g = mh_f = .10\text{ kg}(3.34 \times 10^5\text{ J/kg}) = 33,400$
 $Q_g = mc\Delta t_{wi} = .1\text{ kg}(4180\text{ J/kgC})(74.1 - 0^\circ\text{C}) = +31000\text{ J}$
 $Q_g = +66,500$

100.0 g of ice at -10.0°C is placed in 1.00 kg of water at 90.0°C . What is the final temperature of the mixture?

$Q_L + Q_S = 0$

$$m_c \Delta t_w + m_c \Delta t_i + m h_f + m_c \Delta t_{wi} = 0$$

$$m_c \Delta t_w + m_c \Delta t_{wi} = -m_c \Delta t_i - m h_f$$

$$m_c (t_f - t_i)w + m_c (t_f - t_i)w_i = -m_c (t_i - t_i) - m h_f$$

$$m_c (t_f w - m_c t_i w) + m_c (t_f w_i - m_c t_i w_i) = -m_c \Delta t_i - m h_f$$

$$m_c t_f w + m_c t_f w_i - m_c t_i w - m_c t_i w_i = -m_c \Delta t_i - m h_f$$

$$t_f (m_c w + m_c w_i) = \frac{m_c t_i w + m_c t_i w_i - m_c \Delta t_i - m h_f}{m_c w + m_c w_i}$$

$$t_f = \frac{1 \text{ kg} (4180 \text{ J/kg}) (90) + 1 \text{ kg} (4180 \text{ J/kg}) (0) - (1 \text{ kg}) (2060 \text{ J/kg}) (10) - .1 \text{ kg} (3.34 \times 10^5 \text{ J/kg})}{1 \text{ kg} (4180 \text{ J/kg}) + .1 \text{ kg} (4180 \text{ J/kg})}$$

$$t_f = 74.1^\circ\text{C}$$

$Q_L + Q_S = 0$

$Q = m c \Delta t_w = 66500 \text{ J}$

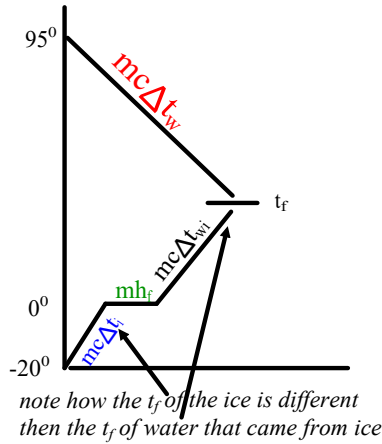
$Q = m c \Delta t_w = 31000 \text{ J}$

$Q = m c \Delta t_i = 20600 \text{ J}$

$t_f = 74.1^\circ$

A 150.0 g block of ice at -20.0°C is placed in 880.0 g of water at 95.0°C . What is the final temperature of the mixture.

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$$Q_L + Q_g = 0$$

$$mc\Delta t_w + mc\Delta t_i + mh_f + mc\Delta t_{wi} = 0$$

$$mc\Delta t_w + mc\Delta t_{wi} = -mc\Delta t_i - mh_f$$

$$mct_{fw} - mct_{iw} + mct_{fwi} - mct_{iwi} = -mc\Delta t_i - mh_f$$

$$mct_{fw} + mct_{fwi} = -mc\Delta t_i - mh_f + mct_{iw} + mct_{iwi}$$

$$t_f(mc_w + mc_{wi}) = -mc\Delta t_i - mh_f + mct_{iw} + mct_{iwi}$$

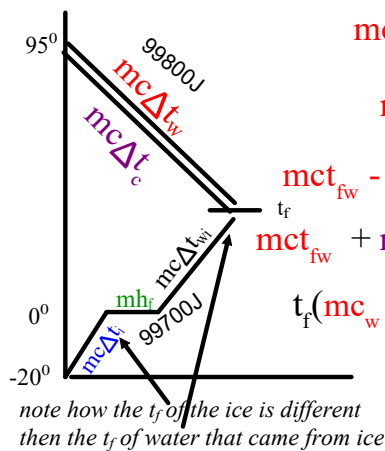
$$t_f = \frac{-mc\Delta t_i - mh_f + mct_{iw} + mct_{iwi}}{(mc_w + mc_{wi})}$$

$$t_f = \frac{-.15 \text{ kg}(2060 \text{ J/kgC})20^{\circ}\text{C} - .15 \text{ kg} (3.34 \times 10^5 \text{ J/kg}) + .88 \text{ kg}(4180 \text{ J/kgC})95^{\circ}\text{C} + .15 \text{ kg}(4180 \text{ J/kgC})0^{\circ}\text{C}}{(.88 \text{ kg}(4180 \text{ J/kgC}) + .15 \text{ kg}(4180 \text{ J/kgC}))}$$

$$t_f = 68.1^{\circ}\text{C}$$

A 150.0 g block of ice at -20.0°C is placed in 880.0 g of water at 95.0°C . What is the final temperature of the mixture. Oh no, the water is in a 225 g aluminum cup!

$$Q_L + Q_g = 0$$



$$mc\Delta t_w + mc\Delta t_c + mc\Delta t_i + mh_f + mc\Delta t_{wi} = 0$$

$$mc\Delta t_w + mc\Delta t_c + mc\Delta t_{wi} = -mc\Delta t_i - mh_f$$

$$mct_{fw} - mct_{iw} + mct_{fc} - mct_{ic} + mct_{fwi} - mct_{iwi} = -mc\Delta t_i - mh_f$$

$$mct_{fw} + mct_{fc} + mct_{fwi} = -mc\Delta t_i - mh_f + mct_{iw} + mct_{ic} + mct_{iwi}$$

$$t_f(mc_w + mc_c + mc_{wi}) = -mc\Delta t_i - mh_f + mct_{iw} + mct_{ic} + mct_{iwi}$$

$$t_f = \frac{-mc\Delta t_i - mh_f + mct_{iw} + mct_{ic} + mct_{iwi}}{(mc_w + mc_c + mc_{wi})}$$

$$t_f = \frac{-.15 \text{ kg}(2060 \text{ J/kgC})20^{\circ}\text{C} - .15 \text{ kg} (3.34 \times 10^5 \text{ J/kg}) + .88 \text{ kg}(4180 \text{ J/kgC})95^{\circ}\text{C} + .225 \text{ kg}(903 \text{ J/kgC})95^{\circ}\text{C} + .15 \text{ kg}(4180 \text{ J/kgC})0^{\circ}\text{C}}{(.88 \text{ kg}(4180 \text{ J/kgC}) + .225 \text{ kg}(903 \text{ J/kgC}) + .15 \text{ kg}(4180 \text{ J/kgC}))}$$

$$t_f = 69.3^{\circ}\text{C}$$

$T E$ needed to change ^{1 kg} water
from $0^\circ C \rightarrow 100^\circ C$

$$Q = mc \Delta t$$

$$Q = mc (t_f - t_i)$$

$$Q = 1 \text{ kg} (4180 \text{ J/kg}^\circ\text{C}) (100^\circ\text{C} - 0^\circ\text{C})$$

$$Q = \cancel{1 \text{ kg}} (4180 \cancel{\text{ J/kg}^\circ\text{C}}) 100^\circ\text{C}$$

$$Q = 418,000 \text{ J}$$

$$P = \frac{Q}{t} \quad t = \frac{Q}{P} = \frac{mc \Delta t_c}{P}$$

$$t_i = 19^\circ\text{C}$$

$$t = \frac{.175 \text{ kg} (3870 \text{ J/kg}^\circ\text{C}) \Delta t}{25 \text{ W}}$$



$$t_f = 40^\circ\text{C}$$

$$P = 25 \text{ W}$$

$$t = ?$$

$$c_c = 3870 \text{ J/kg}^\circ\text{C}$$

$$m = 175 \text{ ml}$$

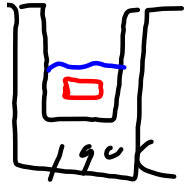
$$t = 5692$$

$$\rightarrow 9.48 \text{ min}$$

$$\rightarrow 175 \text{ g}$$

$$1 \text{ g} = 1 \text{ cm}^3 = 1 \text{ ml}$$

100°C



$$Q_L + Q_S = 0$$

$$m(\Delta t)_m + m(\Delta t)_w + m(\Delta t)_c = 0$$

$$m(\underbrace{t_f - t_i}_m) + m(\underbrace{t_f - t_i}_w) + m(\underbrace{t_f - t_i}_c)$$

